

# Applications of Graph Integration to Function Comparison and Malware Classification

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Cylance Inc.

# Agenda

1. Overview of our Vectorization Method
2. The .NET Framework and Common Language Runtime (CLR)
3. Decompilation
4. Graph Integration
5. Results

# Overview of our Vectorization Method

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4. Compute component-wise mean/std of antiderivatives across all  $G$  resulting from decompilation of the given file

# **The .NET Framework and Common Language Runtime (CLR)**

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- the CLR JITs the code from IL to machine code run on the cpu

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- *Shortsighted Data Flow Graphs* (SDFG) - each obtained by merging all paths through the AST corresponding to a constituent function



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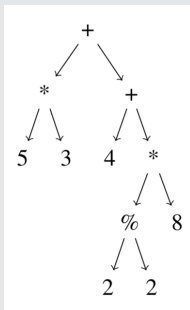
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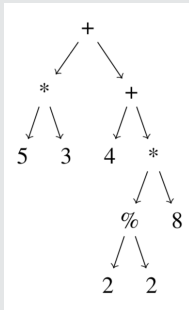
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Distilled semantic structure = order of operations





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Code that when evaluated **does** yield a value. Valid in places such as tests, for loops, conditionals, or as the right-hand side of assignments.

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## Statements

Code that when evaluated **does not** yield a value. E.g., a statement cannot be on the right-hand side of an assignment.

- [Assignment](#) - storage of rh variable to the location yielded by lh variable
- [CLRVariableWithInitializer](#) - declaration and subsequent initialization

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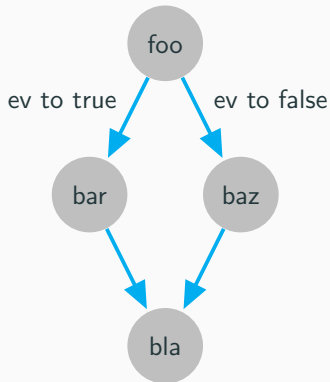
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## Example 2

Consider the set of invertible  $n \times n$  matrices  $GL_n(\mathbb{F})$  on some field  $\mathbb{F}$ . We might choose to study  $GL_n(\mathbb{F})$  by studying

$$\text{tr}, \det : GL_n(\mathbb{F}) \longrightarrow \mathbb{R}$$

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where the PageRank vector is taken to be the steady-state probability distribution over the nodes resulting from the long-run behavior of the random-walk Markov Chain.



# Graph Integration

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A discrete-time *Markov chain* is a sequence of random variables  $X_1, X_2, \dots$  such that

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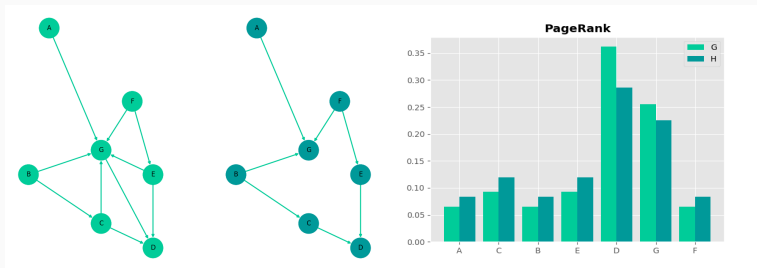
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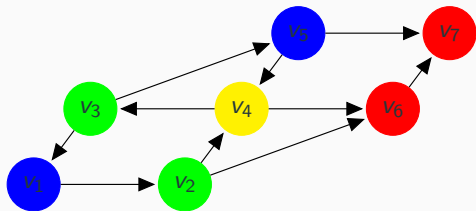
allows us to define our **graph antiderivative**  $F_{f,G}$  of  $f$  by

$$\begin{aligned}F_{f,G} &:= (\nu_f(G_{q_1}), \nu_f(G_{q_2}), \dots, \nu_f(G_{q_{|\mathcal{P}|}})) \\ &= (\mathbb{E}[f|_{G_{q_1}}], \mathbb{E}[f|_{G_{q_2}}], \dots, \mathbb{E}[f|_{G_{|\mathcal{P}|}}])\end{aligned}$$

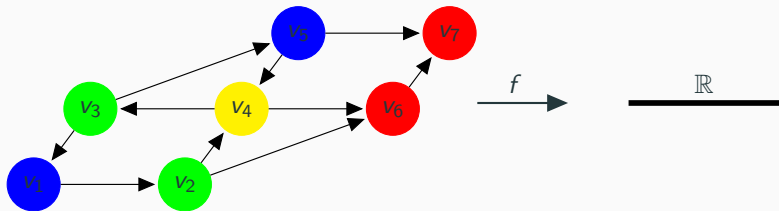


# The Graph Antiderivative Visualized

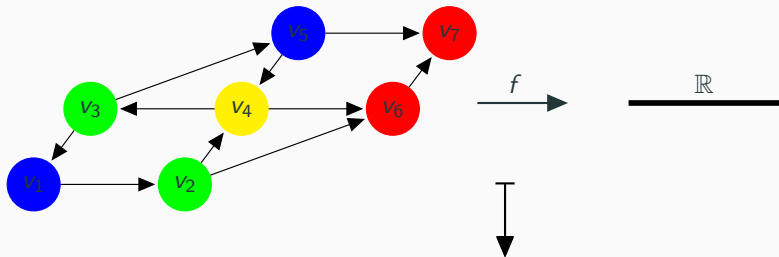
# The Graph Antiderivative Visualized



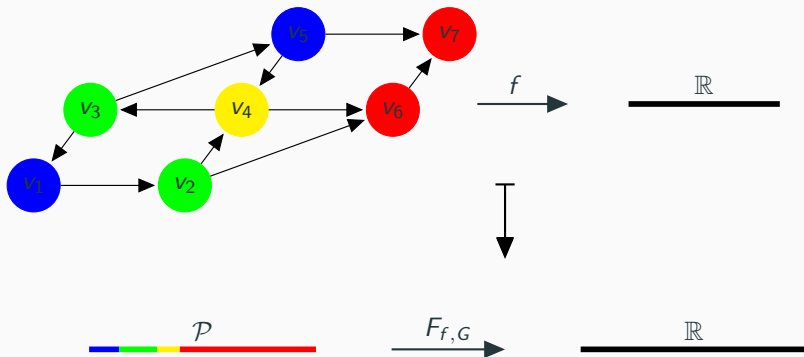
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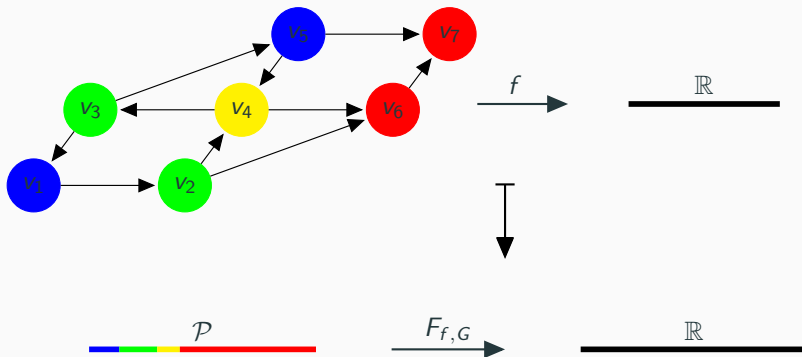
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## Antiderivative

$$\Gamma \times \text{Fun}\left(\bigsqcup_{\Gamma} \text{Vert}(G), \mathbb{R}\right) \longrightarrow \text{Fun}(\mathcal{P}, \mathbb{R})$$

$$(G, f) \mapsto (F_{f,G} : q \mapsto \mathbb{E}[f|_{G_q}]),$$

## Graph Integration: Example

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$$\text{PageRank}(G) = \langle p_{v_1} = 0.10, p_{v_2} = 0.15, p_{v_3} = 0.25, p_{v_4} = 0.50 \rangle$$



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Then  $F_{\text{NumPass2Call}, G} : \mathcal{P} \longrightarrow \mathbb{R}$  takes the form

$$\begin{pmatrix} 0.05 \\ 0.12 \\ 0.95 \end{pmatrix} \mapsto \begin{pmatrix} 0 \\ 0.1 * \#\text{args}_{v_1} \\ 0.1 * \#\text{args}_{v_1} + 0.5 * \#\text{args}_{v_4} \end{pmatrix}$$

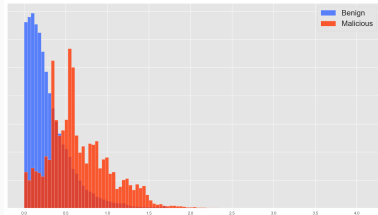
## Results

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# Vectorization Efficacy

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$$\int_0^{0.6} \text{ClassRefname} : v \mapsto \eta(\text{name}(v)) d\mathbb{P}$$

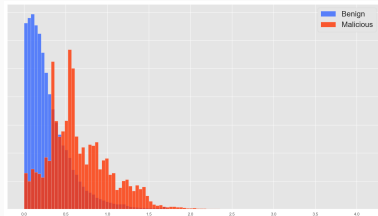


Name of referenced class at  $v$



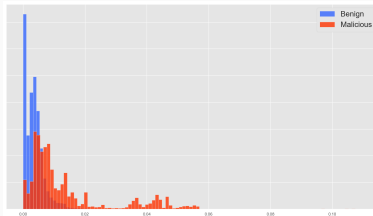
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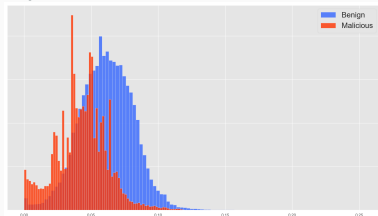
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$$\int_0^{0.4} \text{CLRLiteral} : v \mapsto \eta(\text{type}(v)) d\mathbb{P}$$



Type of literal occurring at  $v$

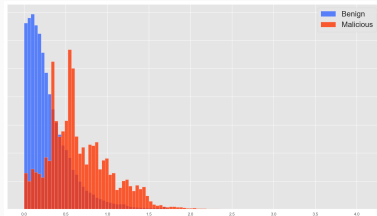
$$\int_0^{0.95} \text{ArgRefType} : v \mapsto \eta(\text{type}(v)) d\mathbb{P}$$



Type of argument referenced at  $v$

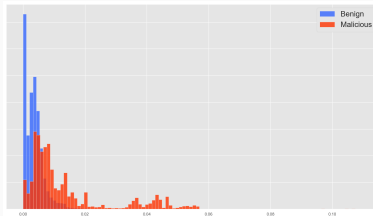
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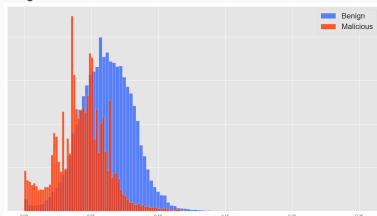
Name of referenced class at  $v$

$$\int_0^{0.4} \text{CLRLiteral} : v \mapsto \eta(\text{type}(v))d\mathbb{P}$$



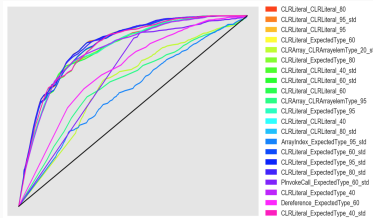
Type of literal occurring at  $v$

$$\int_0^{0.95} \text{ArgRefType} : v \mapsto \eta(\text{type}(v))d\mathbb{P}$$



Type of argument referenced at  $v$

Top Features by AUC



Value/type of literal expression at  $v$

## Model Results - Random Forest

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**Table 1:** Graph Antiderivative-based vectorization

Class	Precision	Recall	F1-score	Support
Benign	97.88%	99.37%	98.62%	696827
Malware	98.94%	96.47%	97.69%	424420
avg/total	98.28%	98.27%	98.27%	1121247
False Positive Rate	1.10%			
False Negative Rate	1.72%			

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**Table 2:** Text-only vectorization

Class	Precision	Recall	F1-score	Support
Benign	90.61%	87.04%	88.79%	696827
Malware	87.80%	91.18%	89.46%	424420
avg/total	89.19%	89.13%	89.13%	1121247
False Positive Rate	8.79%			
False Negative Rate	12.96%			

**Questions?**